

Daily Tutorial Sheet-4

JEE Advanced (Archive)

46.(123 g/ml)

Mass of liquid = 148 – 50 = 98 g

$$\Rightarrow \text{Volume of liquid} = \frac{98}{0.98} = 100 \text{ mL} = \text{volume of flask}$$

Mass of gas = 50.5 – 50 = 0.50 g

Now applying ideal gas equation : $pV = \left(\frac{w}{M}\right)RT$

$$\Rightarrow M = \frac{wRT}{pV} = \frac{0.5 \times 0.082 \times 300}{1 \times 0.1} = 123 \text{ g mol}^{-1}$$

47.(A) A is the measure of intermolecular force of attraction. Greater the intermolecular force of attraction (H-bond in the present case) higher the value of a.

48.(6.46 atm L² mol⁻²)

The van der Waals' equation is $\left(p + \frac{n^2a}{V^2}\right)(V - nb) = nRT$

$$\Rightarrow a = \frac{V^2}{n^2} \left[\frac{nRT}{V - nb} - p \right] = \frac{(4)^2}{(2)^2} \left[\frac{2 \times 0.082 \times 300}{4 - 2(0.05)} - 11 \right] = 6.46 \text{ atm L}^2 \text{ mol}^{-2}$$

49.(0.99 atm)

In case of negligible molecular volume, b = 0 and van der Waals' equation reduces to

$$\left(p + \frac{n^2a}{V^2}\right)V = nRT \Rightarrow p = \frac{RT}{V} - \frac{a}{V^2} = \frac{0.082 \times 273}{22.4} - \frac{3.592}{(22.4)^2} = 0.99 \text{ atm}$$

50.(B) Compressibility factor (Z) = $\frac{V_{\text{real}}}{V_{\text{ideal}}} < 1$ (given)

$$\Rightarrow V = 22.4 \text{ L} \quad \therefore V_{\text{id}} (1 \text{ mol}) = 22.4 \text{ L at STP}$$

51.(C) $u_{\text{rms}} = \sqrt{\frac{3RT}{M}}$

$$\frac{u_{\text{rms}}(\text{H}_2)}{u_{\text{rms}}(\text{N}_2)} = \sqrt{7} = \sqrt{\frac{T_{(\text{H}_2)}}{2} \times \frac{28}{T_{(\text{N}_2)}}}$$

$$7 = \frac{14T_{(\text{H}_2)}}{T_{(\text{N}_2)}} \Rightarrow T_{(\text{N}_2)} = 2T_{(\text{H}_2)} \Rightarrow T_{(\text{H}_2)} < T_{(\text{N}_2)}$$

52.(D) Since constant volume is not given in statement I therefore it is false.

53.(D) $V_{\text{rms}} \propto \frac{1}{\sqrt{d}}$

54.(1.25 atm L² mol⁻²)

In case of negligible molecular volume, b = 0. For 1 mole of gas $\left(p + \frac{a}{V^2}\right)V = RT$

$$\Rightarrow pV + \frac{a}{V} = RT \Rightarrow \frac{pV}{RT} + \frac{a}{VRT} = 1 \quad \left[\because \frac{pV}{RT} = Z \right]$$

$$\Rightarrow Z + \frac{a}{\left(\frac{ZRT}{p}\right)RT} = 1 \Rightarrow Z + \frac{a}{ZR^2T^2} = 1$$

$$\Rightarrow a = \frac{ZR^2T^2(1-Z)}{p} = \frac{0.5(0.082 \times 273)^2(1-0.5)}{100}$$

$$a = 1.25 \text{ atm L}^2 \text{ mol}^{-2}$$

55.(ii) ($2.07 \times 10^{-2} \text{ J}$)

(i) (a) 18 g mol^{-1} (b) 50 L mol^{-1} (c) 1.22 (d) Repulsive

(ii) $2.07 \times 10^{-20} \text{ J}$

$$\frac{r_{\text{gas}}}{r_{\text{O}_2}} = 1.33 = \sqrt{\frac{32}{M_{\text{gas}}}}$$

(i) (a) $M_{\text{gas}} = 18 \text{ g mol}^{-1}$ (b) $V_m = \frac{18}{0.36} = 50 \text{ L mol}^{-1}$

(c) $Z = \frac{pV}{RT} = \frac{1 \times 50}{0.082 \times 500} = 1.22$ (d) $\because Z > 1$, repulsive force is dominating.

(ii) $\bar{E}_k = \frac{3}{2} k_B T = \frac{3}{2} \times 1.38 \times 10^{-23} \times 1000 \text{ J} = 2.07 \times 10^{-20} \text{ J}$

56.(B) When the temperature is increased, surface tension of water decreases because cohesive forces decreases due to increased kinetic energy.

57.(C) $PV = nRT \Rightarrow \frac{V}{T} = \frac{nR}{P} \Rightarrow \frac{V}{T} = \text{constant} \quad \boxed{\frac{V_1}{T_1} = \frac{V_2}{T_2}}$

58.(434 ms)

$$\frac{u_{\text{avg}}}{u_{\text{rms}}} = \sqrt{\frac{8RT}{\pi M}} : \sqrt{\frac{3RT}{M}} = \sqrt{\frac{8}{3\pi}} \Rightarrow u_{\text{rms}} = \sqrt{\frac{3\pi}{8}} u_{\text{avg}} = \sqrt{\frac{3 \times 3.14}{8}} \times 400 = 434 \text{ ms}^{-1}$$

59.(A) Positive deviation corresponds to $Z > 1 \because Z = \frac{pV}{nRT}$, for positive deviation, $\frac{pV}{nRT} > 1$

60.(434 ms)

$$V_{\text{rms}} = \sqrt{\frac{3RT}{M}} \quad V_{\text{avg}} = \sqrt{\frac{8RT}{\pi M}}$$